



Spectral Compression for Remote Sensing Using Principal Component Analysis

Vijay Natraj

Jet Propulsion Laboratory, California Institute of Technology

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Rationale / Need for Speed

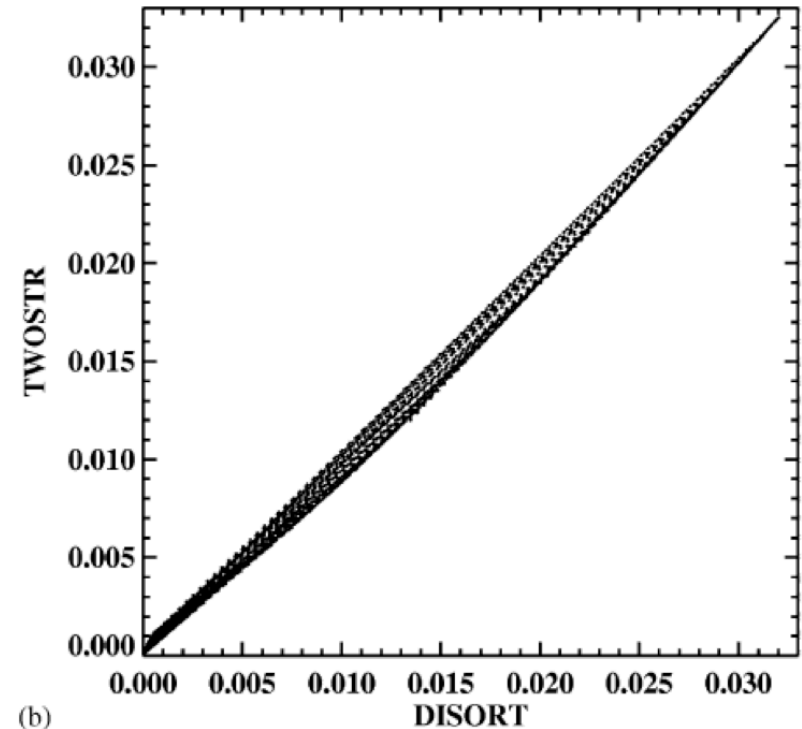
- **RT models required for generating simulated radiances from satellite, ground-based and other platforms**
- **In retrieval applications, RT models also needed to calculate Jacobians**
- **OSSEs and climate models require massive RT modeling over wide spectral ranges**
- **RT calculations computationally expensive**
- **New generation LEO and GEO satellites expected to generate data at rates current computing power is unlikely to match**

Why is RT Computationally Expensive?

- **Wavelengths**
 - Spectral points where radiances must be evaluated
- **Angles**
 - Computational quadrature angles (“streams”) at each spectral point
- **A good solution should address BOTH the above considerations.**

Angles

- Separation of single and multiple scattering
 - Large number (sometimes $\gg 100$) of streams required to resolve accurately anisotropy due to scattering
 - Computational burden $\sim O(M^3)$
 - Large part of anisotropy of radiation field captured by single scattering
 - Single scattering calculation computationally efficient
- Correlation between multi-stream and two-stream calculations



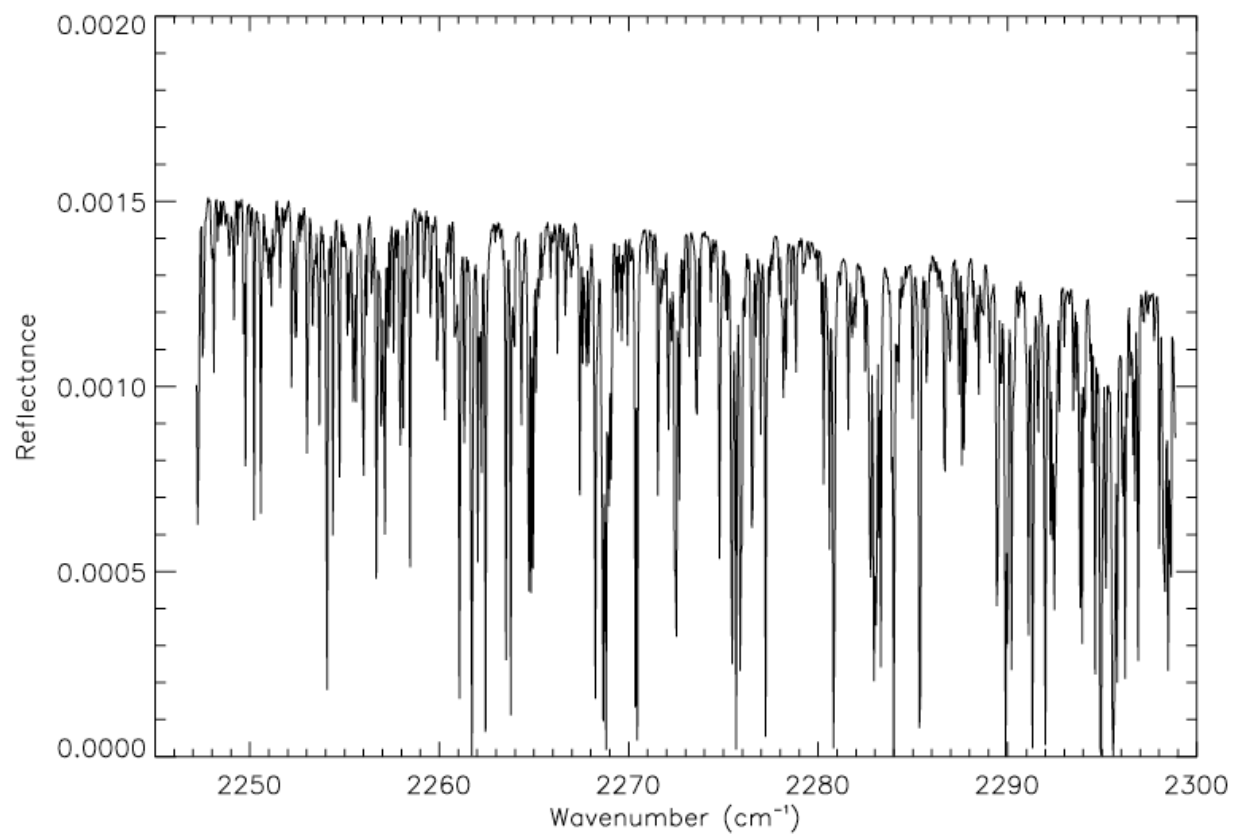
Natraj et al., 2005

$$I_{PCA}(\lambda) = [I_{2S}(\lambda)]C(\lambda) + \bar{I}_{FO}(\lambda)$$

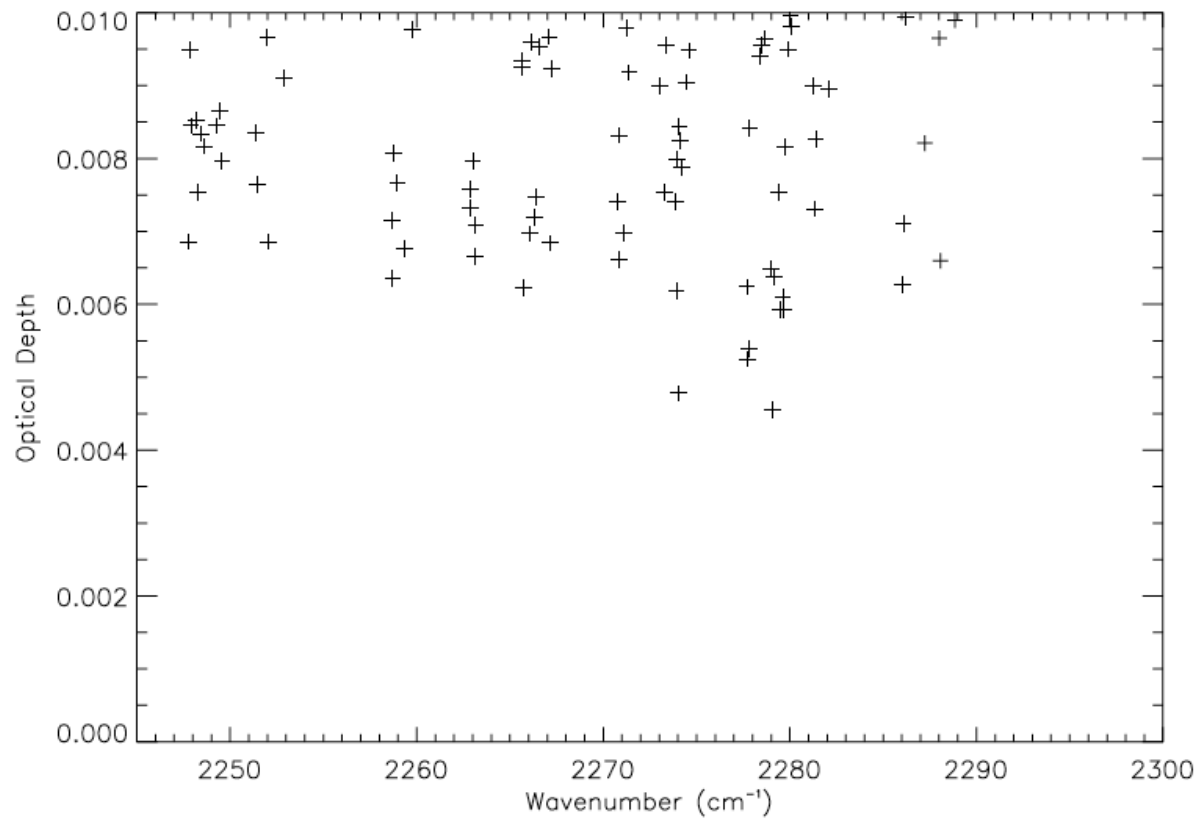
Wavelengths

- **Spectral binning**
- **Eigenvalue problem solution**
- **Radiance back-mapping**

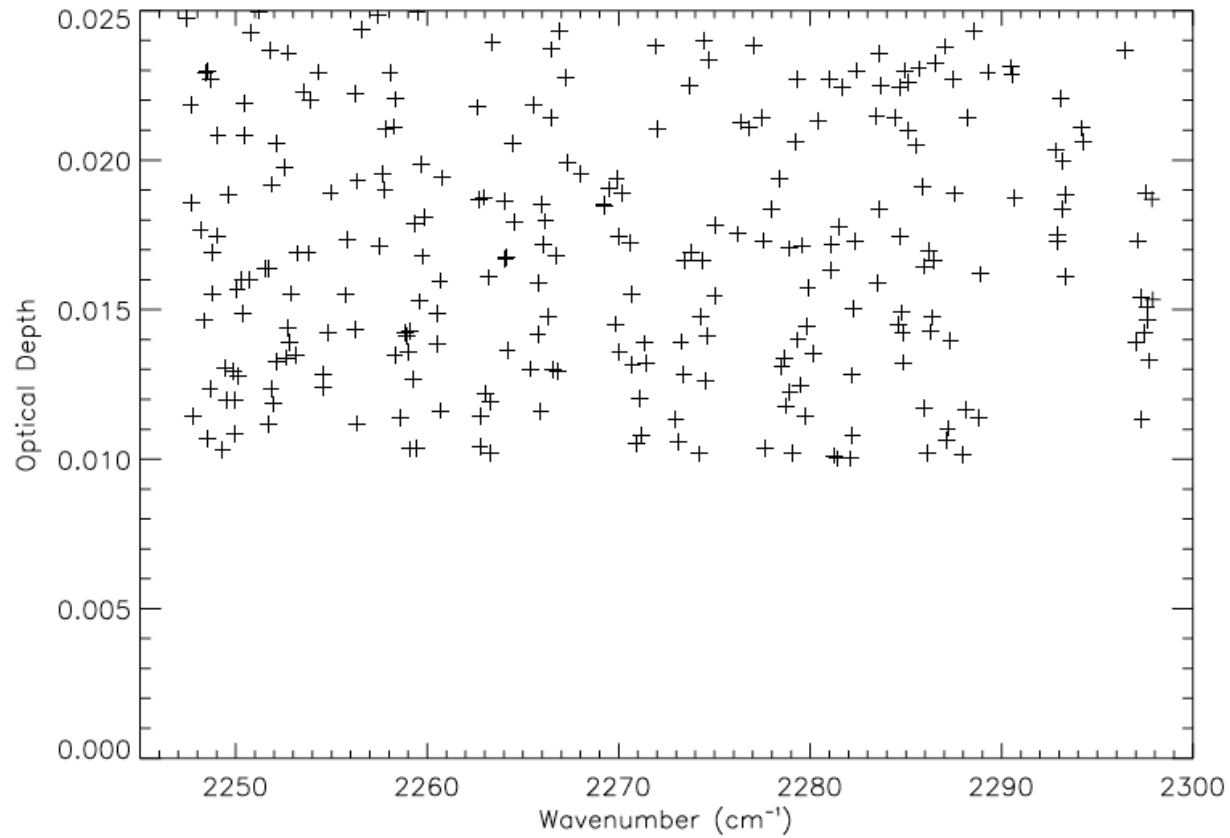
Spectral Binning



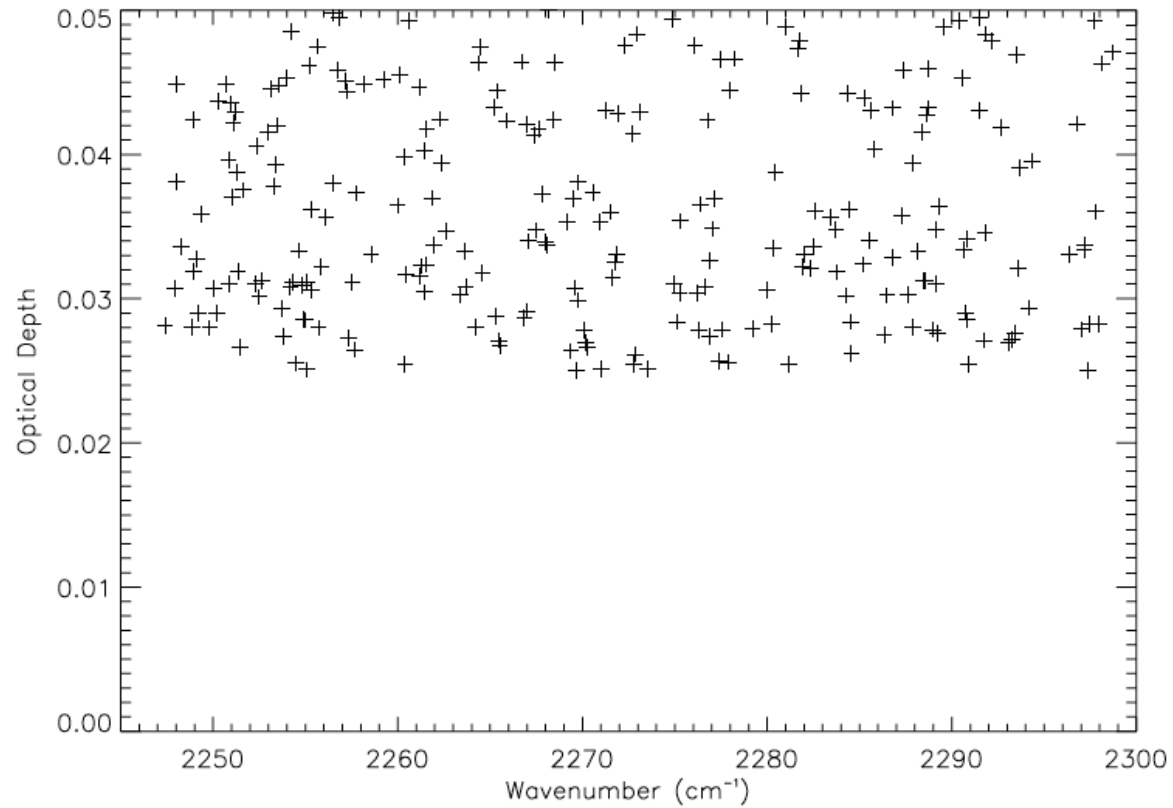
Spectral Binning



Spectral Binning

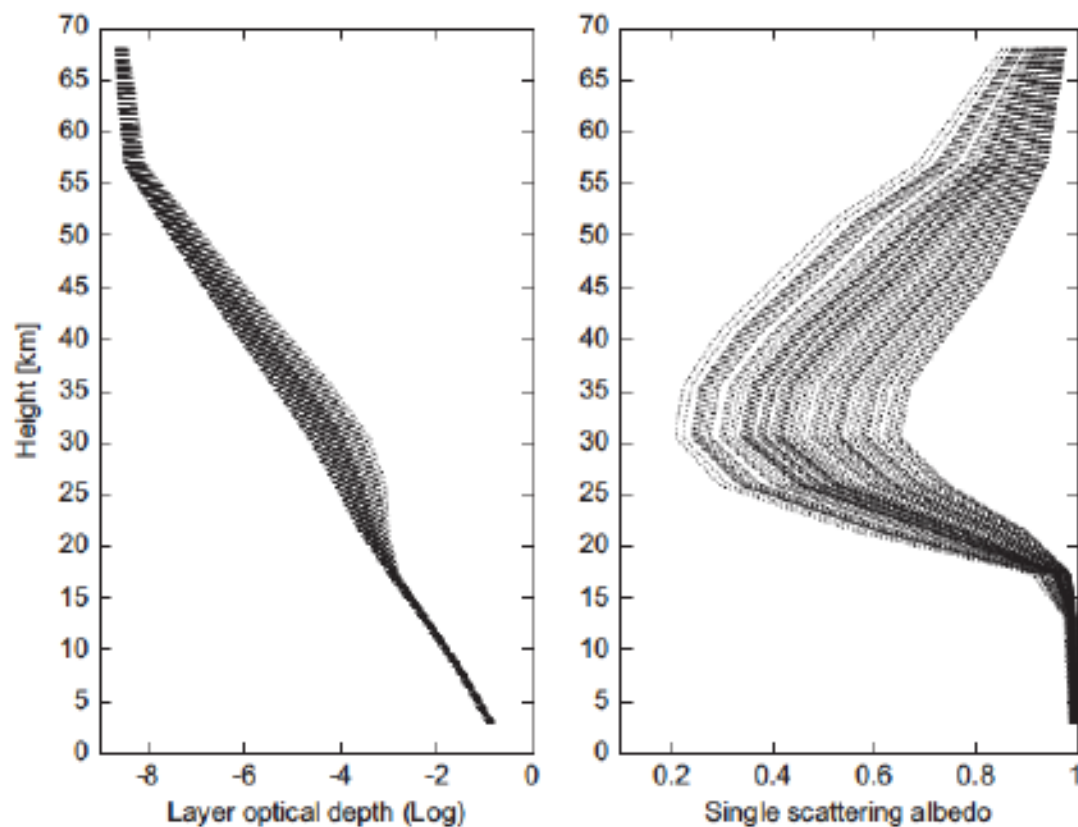


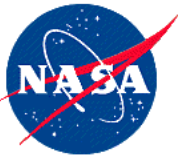
Spectral Binning





RT Data Set





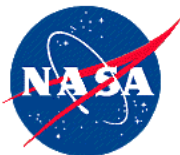
Eigenvalue Problem Solution: PCA

- **Data Set**
 - Optical properties in M atmospheric layers at N wavelengths
- **Empirical Orthogonal Functions (EOFs)**
 - Eigenvectors of covariance matrix of detrended (mean removed) data set
 - New basis to represent original data
 - No loss of information
- **Principal Component Scores/Weights**
 - Projection of original data set onto EOFs



Eigenvalue Problem Solution: PCA

- **PCA is an orthogonal transformation**
- **EOFs uncorrelated (original data set strongly correlated)**
- **EOFs sorted in order of decreasing variance accounted for**
- **First few (typically ≤ 4) EOFs capture $> 99.99\%$ of variance**
- **PCA gives insight into variability patterns in data sets**



Eigenvalue Problem Solution: PCA

- **Mean and EOFs define much smaller set of PCA-projected optical states compared to original data set**
- **Multiple scattering (MS) simulations performed only on reduced set**
- **Fast two-stream model approximates MS contribution at each spectral point**
- **Correction factors developed based on RT calculations at PCA-projected optical states**
- **Single scatter calculations performed at each spectral point**



Radiance Back-Mapping

- Radiances for mean bin values: I_{exact} , I_{2S}

$$I_d = \ln(I_{exact}/I_{2S})$$

- EOF-perturbed ratios: I_d^+ , I_d^-
- First and second order differences

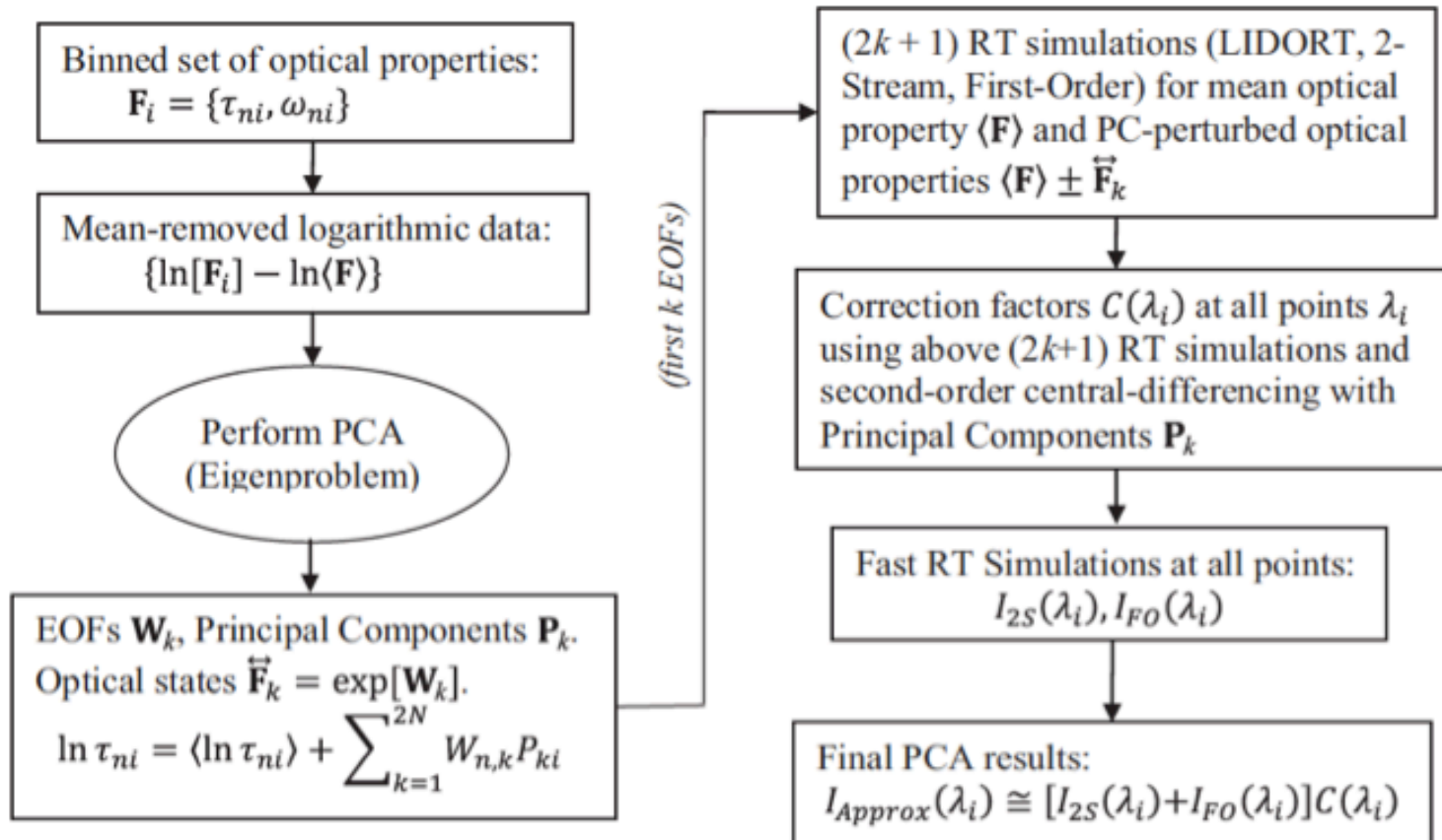
$$\delta I_k = \frac{I_d^+ - I_d^-}{2}$$

$$\delta^2 I_k = I_d^+ + I_d^- - 2I_d$$

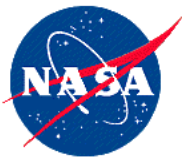
- Corrected MS radiance

$$I_l = I_l^{2S} \exp \left[I_d + \sum_{k=1}^4 \delta I_k P_{k,l} + \frac{1}{2} \sum_{k=1}^4 \delta^2 I_k P_{k,l}^2 \right]$$

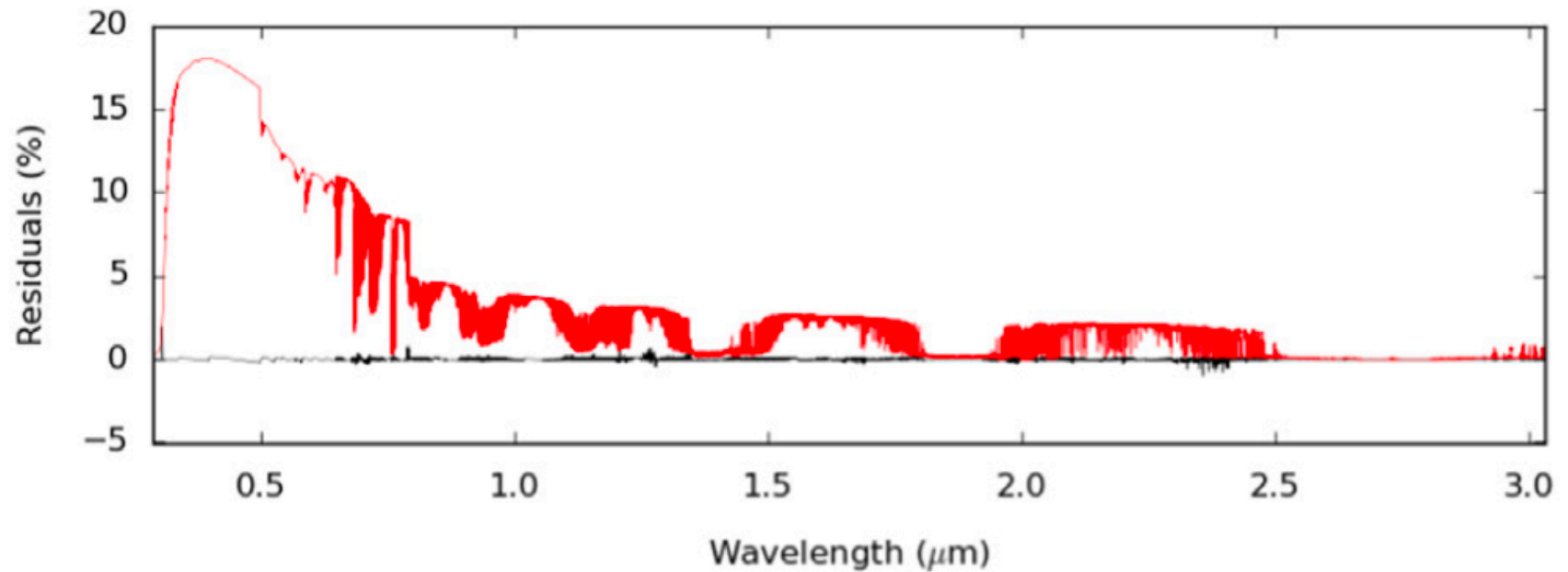
PCA Flowchart



Spurr et al., 2013



Broadband Radiances

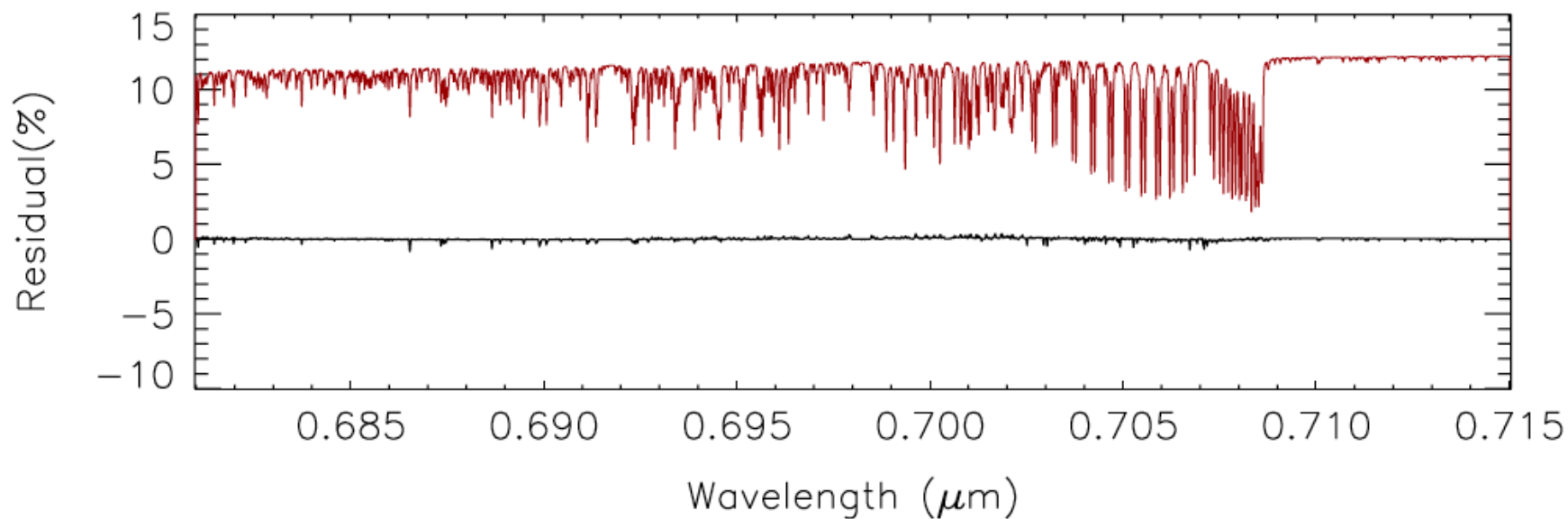


Red: Two-stream; Black: PCA

Kopparla et al., 2016



Zoomed in



Brown: Two-stream; Black: PCA

Kopparla et al., 2016

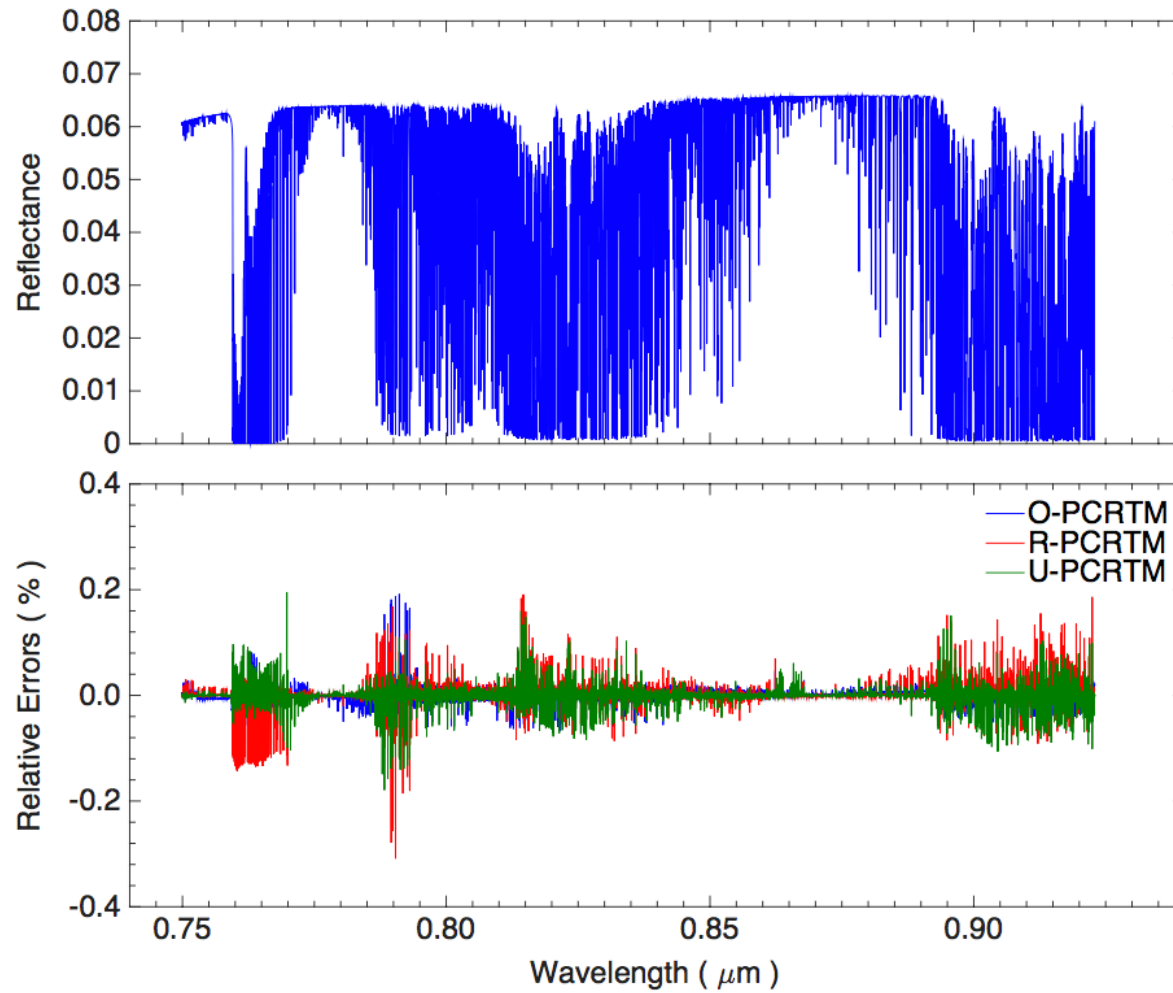
Radiance-Based PCA (Liu, X., et al.)

- **# independent pieces of information << # channels**
- **PCA performed on channel radiances**
- **Large number of atmospheric profiles used to generate a matrix of spectral channel radiances (done offline)**
- **PCA produces EOFs (which are scenario independent)**
- **PC scores for specific scenario obtained using monochromatic calculations at selected wavelengths**

Unified PCA

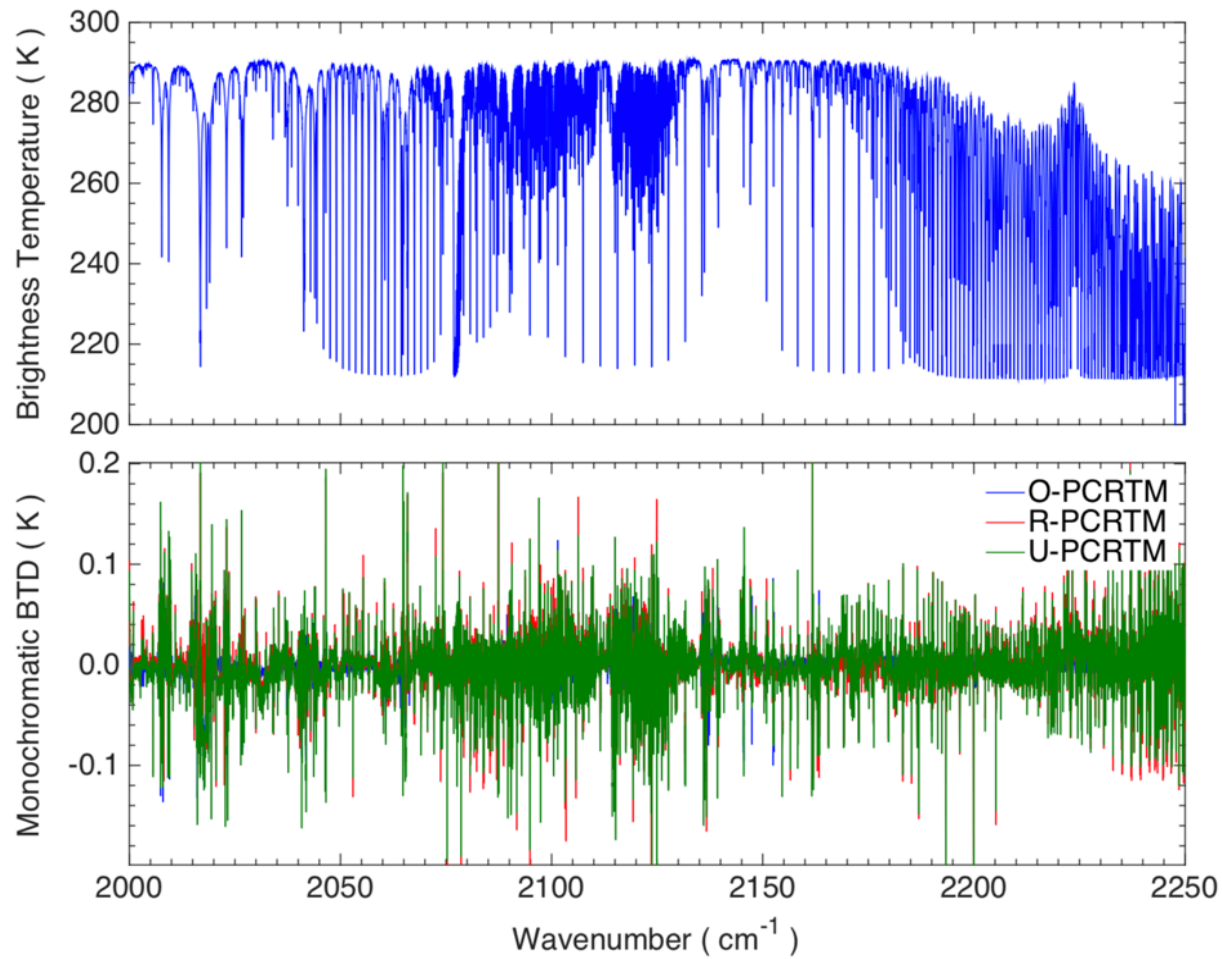
- **Optical-PCA minimizes number of RT calculations per instrument channel**
- **Radiance-PCA minimizes number of instrument channels for which RT calculations are performed**
- **Two techniques are complementary**
- **Unified PCA model would combine advantages of both methods**

Unified PCA Example 1



Liu et al., 2019

Unified PCA Example 2



Liu et al., 2019

Future Work

- **Vertical layering**
- **Spectral sampling**
- **Binning**
- **Polarization**
- **Unified PCA**
- **Remote sensing retrievals / climate models**

Backup Slides

Overview of Existing Techniques I

- **Correlated-k/Exponential Sum Fitting of Transmittances**
 - **Widely used for atmospheric heating/cooling rate calculations**
 - **Assume that optical properties spectrally correlated at all points along optical path**
 - **Only valid for homogeneous, isobaric, isothermal atmospheres**
 - **Loss of correlation can introduce significant radiance errors**

Overview of Existing Techniques II

- **Spectral Mapping**

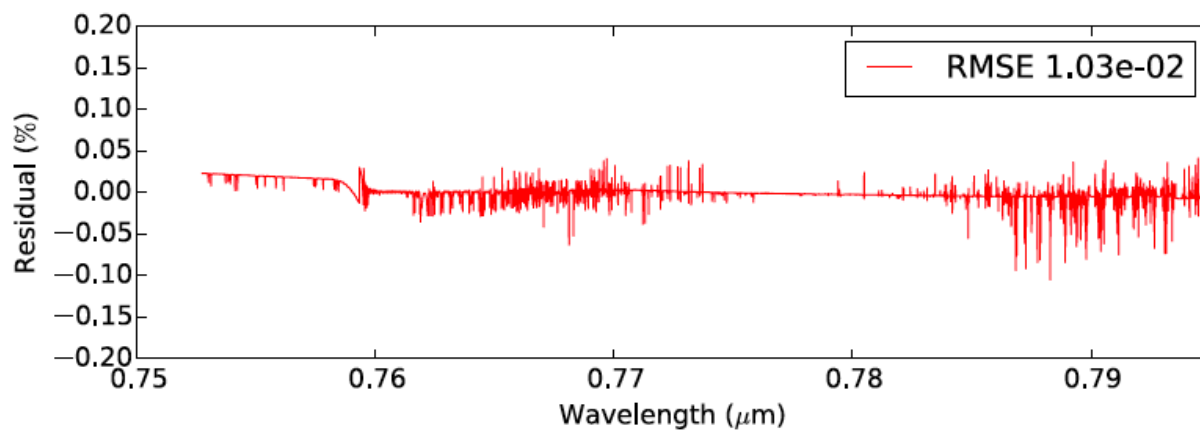
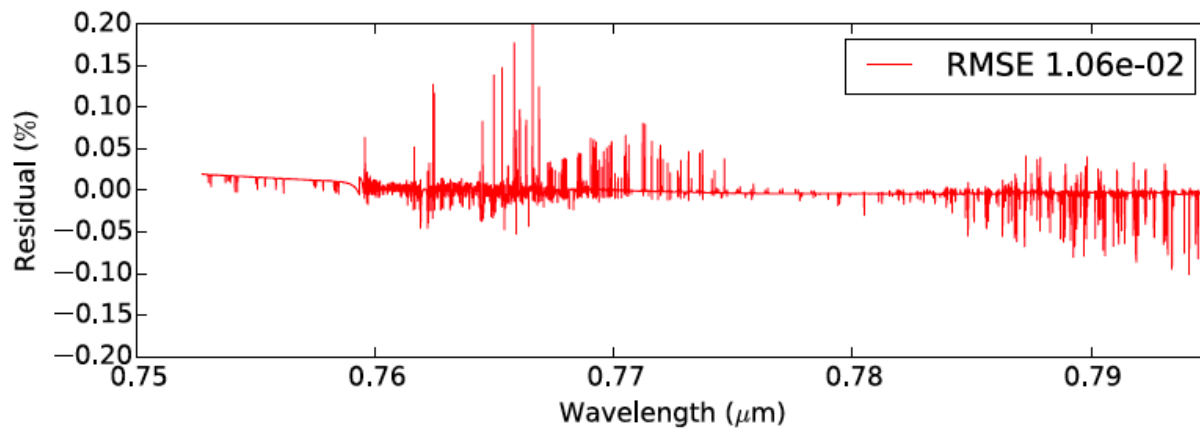
- No assumption about spectral correlation along optical path
- Perform level-by-level comparison of monochromatic atmospheric and surface optical properties
- Combine only spectral regions that remain similar at all points along inhomogeneous optical path
- Fine binning required to achieve high RT calculation accuracy
- Coarse binning provides significant reduction in radiance accuracy

Overview of Existing Techniques III

- **Asymptotic Methods**
 - Limited to study of semi-infinite media (e.g. optically thick clouds)
- **Low Orders of Scattering**
 - Restricted to study of optically thin atmospheres
- **Others**
 - Usefulness only proven for narrow spectral regions
 - Many of these techniques rely on finite differences

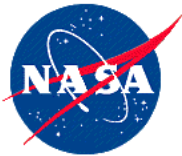


Vertical Grid

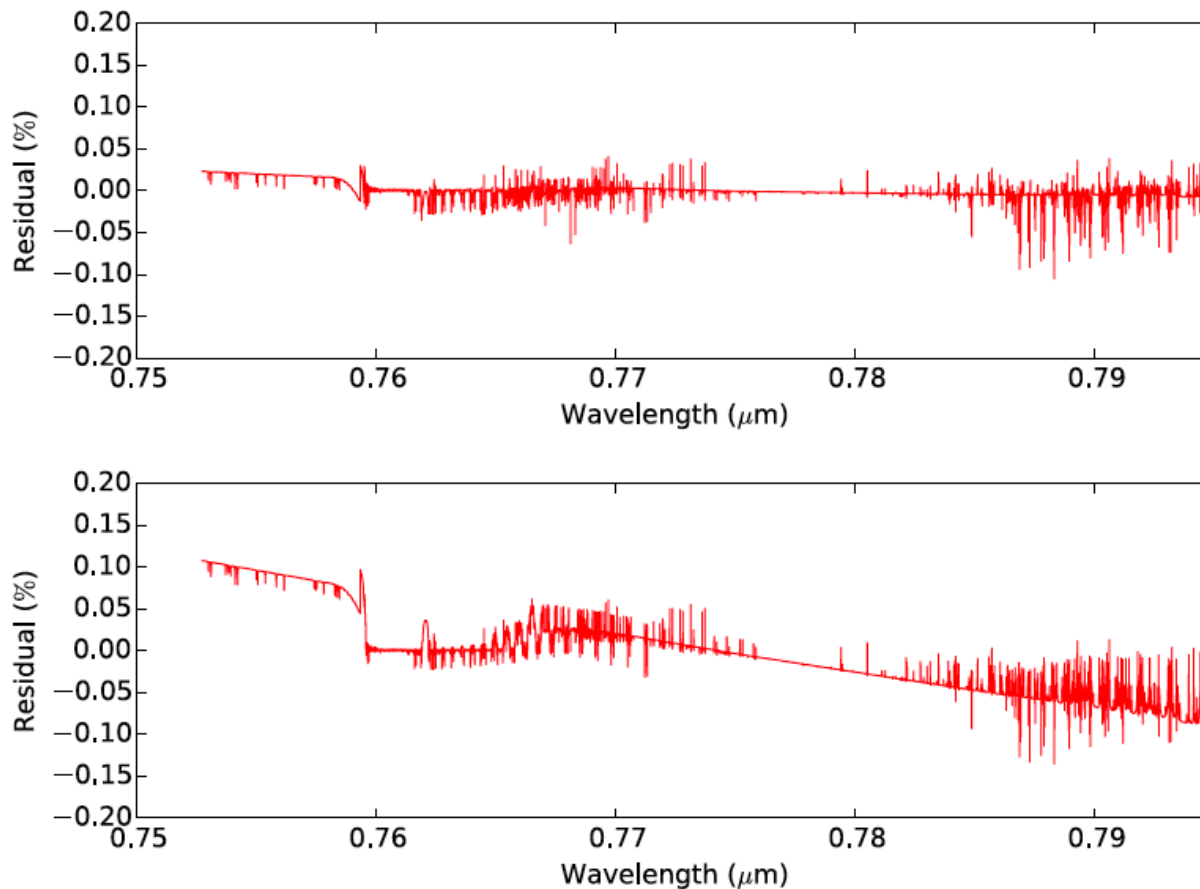


Top: Arbitrary grid; Bottom: Equal pressure thickness grid

Kopparla et al., 2017



Aerosols in the PCA

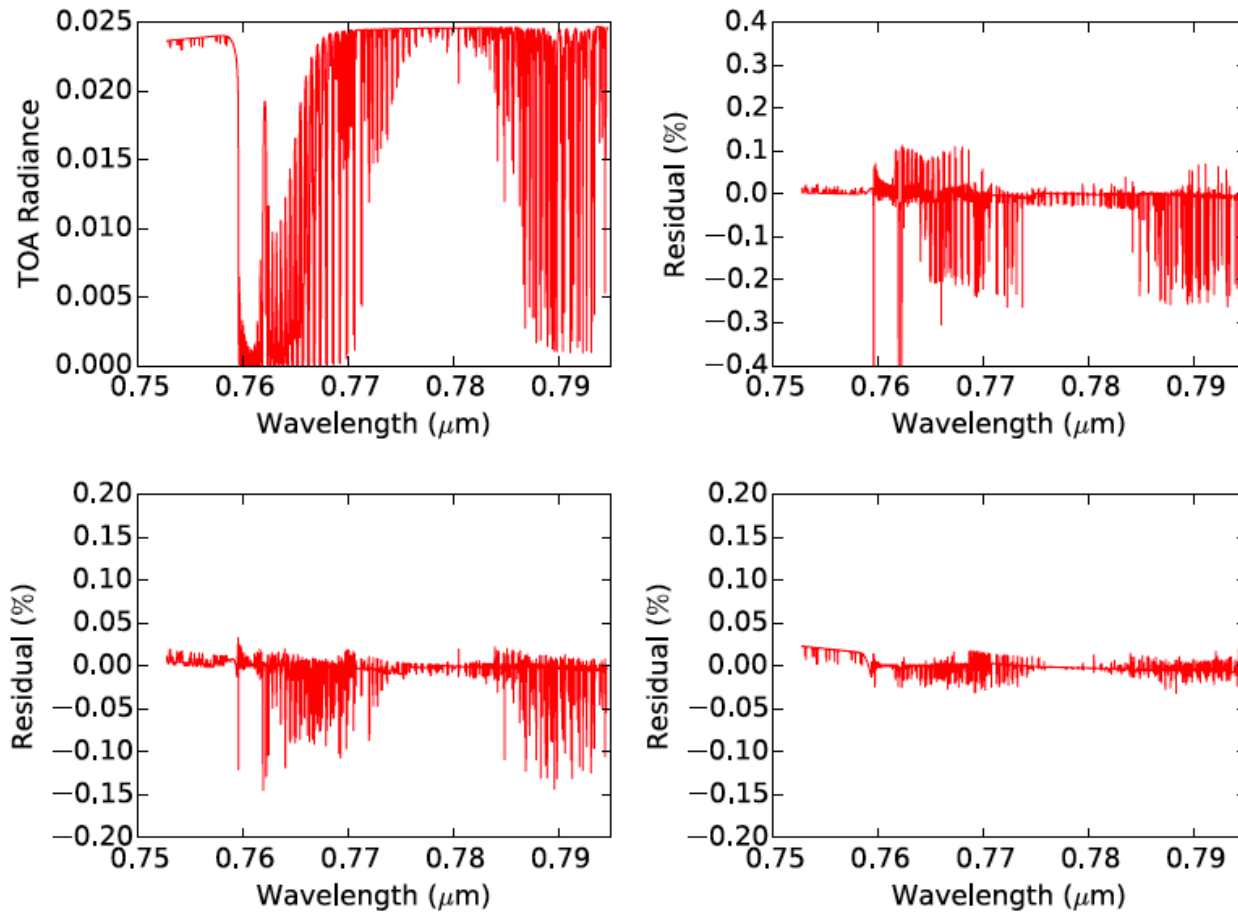


Bottom: Bin averaging for aerosol properties; Top: Aerosols in the PCA

Kopparla et al., 2017

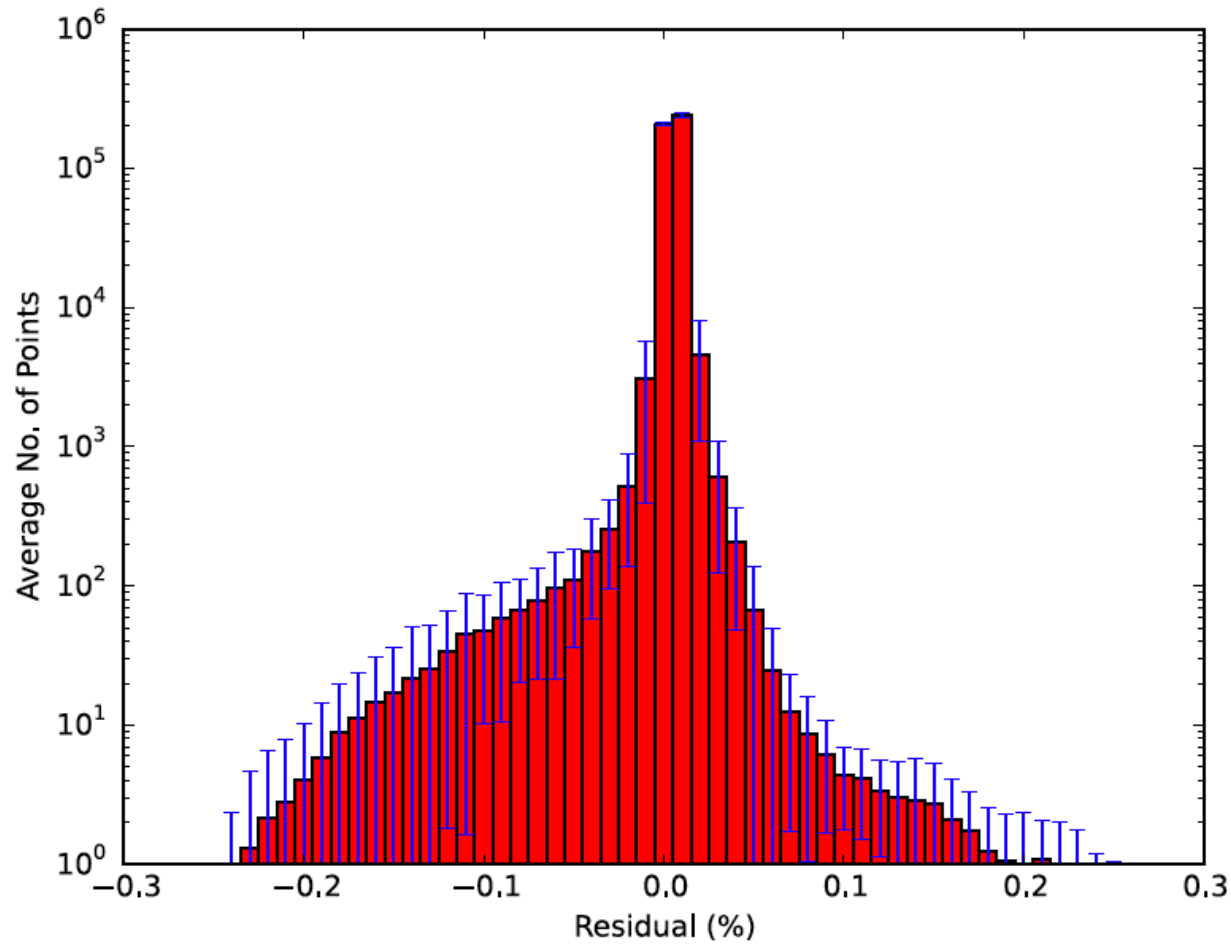


Binning Schemes



Kopparla et al., 2017

Distribution of Residuals



Kopparla et al., 2017